## Title: So Many Possibilities! (The Multiplication Rule)



Standard(s) Addressed in Lesson
Use Math to Solve Problems and Communicate

## Benchmark(s) Addressed in Lesson

M.4.15 Identify, extend and construct arithmetic/geometric patterns and sequences that are one-step and linear or exponential.
M.4.23 Determine, using the fundamental counting principle (multiplication rule), the number of possible outcomes for a situation.
M.4.28 Confirm results with a calculator.
M.4.34 Apply mathematical ideas across a variety of settings (community, family, work).

Materials

- "So Many Possibilities!" worksheet
- calculator

Learner Prior Knowledge
multiplication
Activities
Step 1 Distribute the "So Many Possibilities!" worksheet. Explain the Multiplication Rule and read through the examples.

Step 2 Students solve the problems on the back of the worksheet. They may use a calculator as needed.
Step 3 Check answers for correctness, and save their work in their portfolios as documentation for the Basic Skills Stackable Certificate.
Assessment/Evidence
Completed worksheet
Adaptations for Beginning Students
Beginning students may work with a partner.
Adaptations for Advanced Students
Teacher Reflection/Lesson Evaluation

People are often faced with choices. The number of possible outcomes for any choice is dependent upon the number of possibilities contained within the choice.

## Example 1

Jean works in a doctor's office. She must wear scrubs to work each day. She has four differently patterned scrubs shirts (S1, S2, S3, and S4) and three solid colored scrubs pants (blue, gray, and green). How many possible outfits can she make using only these clothes?

The possible outcomes could be listed in a table and counted.

| S1 Blue | S2 Blue | S3 Blue | S4 Blue |
| :--- | :--- | :--- | :--- |
| S1 Gray | S2 Gray | S3 Gray | S4 Gray |
| S1 Green | S2 Green | S3 Green | S4 Green |

This problem can also be solved by multiplication. Determine the number of possibilities in each option. Then multiply the number of possibilities in each option together to determine the total number of possible outcomes.

| S1 | 1 |  |
| :--- | :--- | :--- |
| S2 | 1 | Blue 1 |
| S3 | 1 | Gray 1 |
| S4 | 1 | Green 1 |
| $--------------------------------~$ |  |  |
| 4 shirt options | x | 3 pants options $=12$ possible outfits |

This is called the Multiplication Rule because one multiplies the number of possibilities for each option together to determine the total number of possible outcomes.

If there are a large number of options in a given situation, it becomes difficult to list and count all of the possible outcomes. Therefore, it is easier to use the Multiplication Rule.

Consider the above scenario if Jean has 12 scrubs shirts and 7 pairs of scrubs pants.
To find the number of possible outfits (outcomes), multiply the number of options in part one (shirts) by the number of options in part two (pants). $12 \times 7=84$ possible outfits

## Example 2

If Ohio creates a new series of license plates that are 2 letters followed by 5 numbers, how many license plates can be created?

For each letter, there are 26 possible choices. For each numeral, there are 10 possibilities (single digits from 0 to 9 ).

| Letter 1 | Letter 2 | Numeral 1 | Numeral 2 | Numeral 3 | Numeral 4 | Numeral 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 26 | 26 | 10 | 10 | 10 | 10 | 10 |

To find the total number of possible outcomes (license plates), multiply the number of possibilities for each option together.

$$
26 * 26 * 10 * 10 * 10 * 10 * 10=676 * 100,000=676,000,000
$$

## Practice

1. This Election Day, your community will elect five new officials. A Democrat, a Republican, and a third party candidate are running for each position. How many possible combinations of officers can be elected to office?
2. You are feeling lucky and you buy a "Pick 4" lottery ticket on your way home from work. How many combinations of numbers are possible?
3. Your family is planning a cross-country bus tour beginning in New York City; stopping in Cincinnati, St. Louis, and Denver; and ending in San Francisco. There are three routes from NYC to Cincinnati, two routes from Cincinnati to St. Louis, four routes from St. Louis to Denver, and three routes from Denver to San Francisco. How many different tour routes are possible?

The Multiplication Rule becomes a little more complicated if some of the choices are reduced. For example, if you are buying a "Pick 4" lottery ticket but are not allowed to choose the same number more than once, you have fewer possibilities.

| Number 1 | Number 2 | Number 3 | Number 4 |
| :---: | :---: | :---: | :---: |
| 10 choices (0-9) | 9 choices | 8 choices | 7 choices |

$$
10 * 9 * 8 * 7=5040
$$

## Challenge

4. How many possible license plates could be created if Ohio used three unique letters and three unique numbers?

People are often faced with choices. The number of possible outcomes for any choice is dependent upon the number of possibilities contained within the choice.

## Example 1

Jean works in a doctor's office. She must wear scrubs to work each day. She has four differently patterned scrubs shirts (S1, S2, S3, and S4) and three solid colored scrubs pants (blue, gray, and green). How many possible outfits can she make using only these clothes?

The possible outcomes could be listed in a table and counted.

| S1 Blue | S2 Blue | S3 Blue | S4 Blue |
| :--- | :--- | :--- | :--- |
| S1 Gray | S2 Gray | S3 Gray | S4 Gray |
| S1 Green | S2 Green | S3 Green | S4 Green |

This problem can also be solved by multiplication. Determine the number of possibilities in each option. Then multiply the number of possibilities in each option together to determine the total number of possible outcomes.

| S1 | 1 |  |
| :--- | :--- | :--- |
| S2 | 1 | Blue 1 |
| S3 | 1 | Gray 1 |
| S4 | 1 | Green 1 |
| $--------------------------------~$ |  |  |
| 4 shirt options | x | 3 pants options $=12$ possible outfits |

This is called the Multiplication Rule because one multiplies the number of possibilities for each option together to determine the total number of possible outcomes.

If there are a large number of options in a given situation, it becomes difficult to list and count all of the possible outcomes. Therefore, it is easier to use the Multiplication Rule.

Consider the above scenario if Jean has 12 scrubs shirts and 7 pairs of scrubs pants.
To find the number of possible outfits (outcomes), multiply the number of options in part one (shirts) by the number of options in part two (pants). $12 \times 7=84$ possible outfits

## Example 2

If Ohio creates a new series of license plates that are 2 letters followed by 5 numbers, how many license plates can be created?

For each letter, there are 26 possible choices. For each numeral, there are 10 possibilities (single digits from 0 to 9 ).

| Letter 1 | Letter 2 | Numeral 1 | Numeral 2 | Numeral 3 | Numeral 4 | Numeral 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 26 | 26 | 10 | 10 | 10 | 10 | 10 |

To find the total number of possible outcomes (license plates), multiply the number of possibilities for each option together.

$$
26 * 26 * 10 * 10 * 10 * 10 * 10=676 * 100,000=676,000,000
$$

## Practice

1. This Election Day, your community will elect five new officials. A Democrat, a Republican, and a third party candidate are running for each position. How many possible combinations of officers can be elected to office?

$$
3 * 3 * 3 * 3 * 3=243
$$

2. You are feeling lucky and you buy a "Pick 4" lottery ticket on your way home from work. How many combinations of numbers are possible?

$$
10 * 10 * 10 * 10=10,000
$$

3. Your family is planning a cross-country bus tour beginning in New York City; stopping in Cincinnati, St. Louis, and Denver; and ending in San Francisco. There are three routes from NYC to Cincinnati, two routes from Cincinnati to St. Louis, four routes from St. Louis to Denver, and three routes from Denver to San Francisco. How many different tour routes are possible?

$$
3 * 2 * 4 * 3=72
$$

The Multiplication Rule becomes a little more complicated if some of the choices are reduced. For example, if you are buying a "Pick 4" lottery ticket but are not allowed to choose the same number more than once, you have fewer possibilities.

| Number 1 | Number 2 | Number 3 | Number 4 |
| :---: | :---: | :---: | :---: |
| 10 choices (0-9) | 9 choices | 8 choices | 7 choices |

$$
10 * 9 * 8 * 7=5040
$$

## Challenge

4. How many possible license plates could be created if Ohio used three unique letters and three unique numbers?

| Letter 1 | Letter 2 | Letter 3 | Number 1 | Number 2 | Number 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 26 | 25 | 24 | 10 | 9 | 8 |

$$
26 * 25 * 24 * 10 * 9 * 8=11,232,000
$$

